# Merging NNLO with Parton Shower

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### Questions

Why do NNLO ?

Why do Parton Shower?

### Questions

Why do NNLO ?

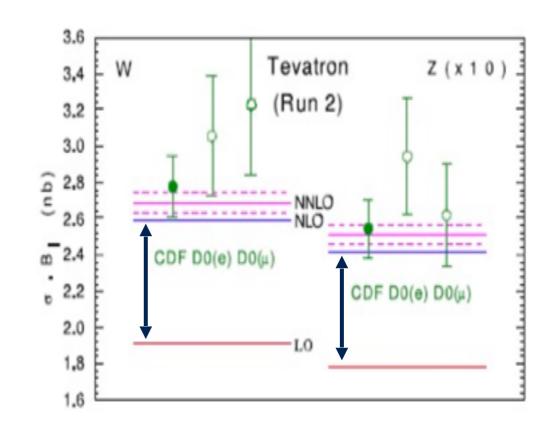
Quantitative predictive power only starts at NLO; need NNLO for high precision

Why do Parton Shower?

# Need Higher Order

Campbell, Ellis, Williams arXiv: 1105.0020

$\sqrt{s}$ [TeV]	$\sigma^{LO}(W^+Z)$ [pb]	$\sigma^{NLO}(W^+Z)$ [pb]
7	6.93(0)	$11.88(1)_{-4.2\%}^{+5.5\%}$
8	8.29(1)	$14.48(1)_{-4.0\%}^{+5.2\%}$
9	9.69(1)	$17.18(1)_{-3.9\%}^{+4.9\%}$
10	11.13(1)	$19.93(1)_{-3.7\%}^{+4.8\%}$
11	12.56(1)	$22.75(2)_{-3.5\%}^{+4.5\%}$
12	14.02(1)	$25.63(2)_{-3.3\%}^{+4.3\%}$
13	15.51(2)	$28.55(2)_{-3.2\%}^{+4.1\%}$
14	16.98(2)	$31.50(3)_{-3.0\%}^{+3.9\%}$



Quantitative predictive power only starts at NLO

# Status of NLO

disclaimer: not a complete list personally biased

- Rapid progress towards full automation: GoSam,
   OpenLoop, MadLoop, ...
  - Thanks to newly developed techniques such as Unitarity method, OPP etc.

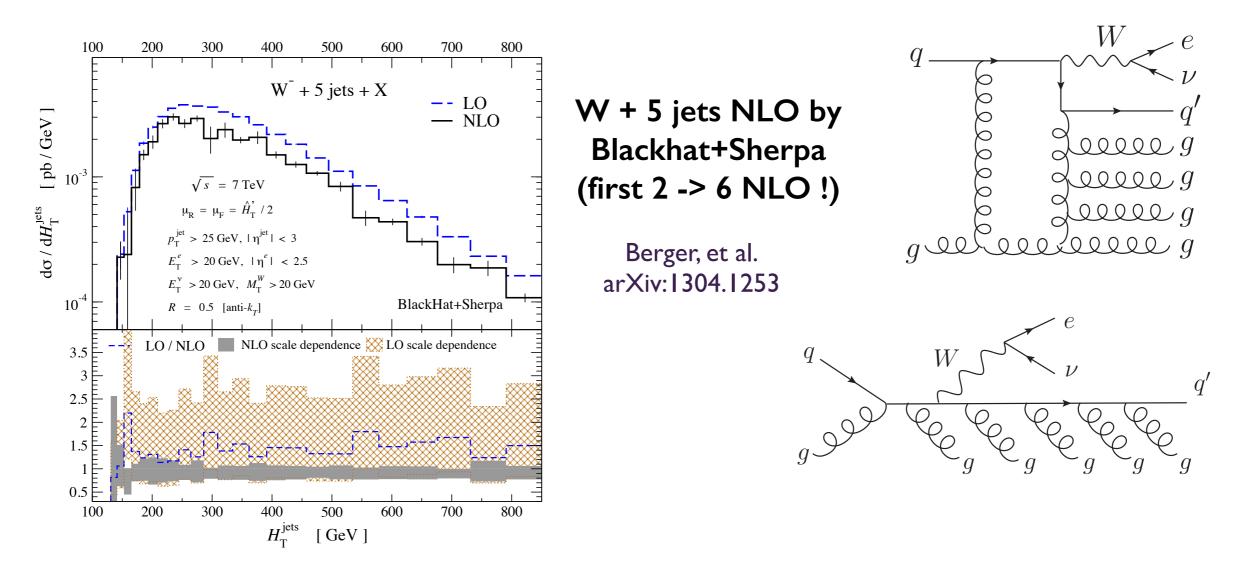
Bern, Dixon, Dunbar, Kosower; Ossola, Papadopoulos, Pittau; Ellis, Giele, Kunszt, Melnikov, ...

Tools for tensor integral reduction: GOLEM, Collier, ...

Denner, Dittmaier; Binoth, Guillet, Pilon, Heinrich, Schuber; ...

- Tools for OPP based reduction: CutTool, Samurai, Ninja ...
- Unitarity method: Blackhat

## Status of NLO

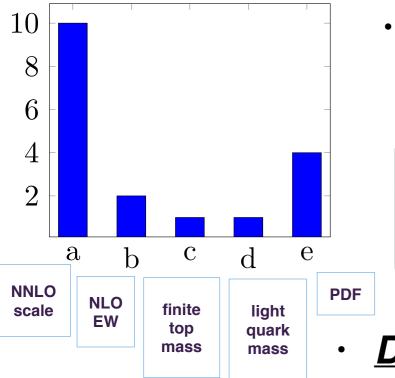


- Even more impressive when it comes to multi-leg NLO calculation
  - Number of diagrams increases factorially with each additional final state particle

## Status of NNLO

Study at LHC mandates precision of NNLO and beyond





the focus of

this talk

- Especially needed for Higgs!
  - projected experimental uncertainty at percent level, while NLO K-factor ~ 2

CMS snowmass workgroup report

$L \text{ (fb}^-1)$	$\gamma\gamma$	WW	ZZ	$b\overline{b}$
300	[6%, 12%]	[6%, 11%]	[7%, 11%]	[11%, 14%]
3000 <	[4%, 8%]	[4%, 7%]	[4%, 7%]	[5%, 7%]

#### **Drell-Yan and Higgs** @ NNLO known for a while

Harlander, Kilgore; Anastasiou, Melnikov; Ravindran, Smith, van Neerven Hamberg, van Neerven, Matsuura

Both color singlet production: simple b/c QCD correction in initial state only

# Intro: Higgs via Gluon Fusion

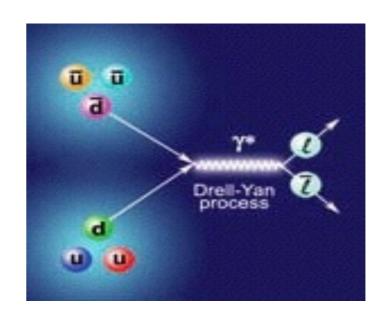


- Finally found Higgs ... need to know if it is SM-like
  - Best prediction from the SM bears ≈15% theoretical uncertainty even at NNLO
    - N3LO calculation well underway; recently results at threshold becomes available
       Anastasiou, Duhr, Dulat, Furlan, Gehrmann, Herzog, Mistlberger YL, Manteuffel, Schabinger, Zhu
  - Mixed EW QCD correction at NNLO worked out in 2008, suggests a good approximation using factorized approach in combining EW and QCD corrections
     Actis, Passarino, Sturm, Uccirati Anastasiou, Boughezal, Petriello
  - Gluon Higgs effective coupling calculated to 5 loops in infinite top
    mass limit (2005); full top mass effect known up to NLO, and NNLO top
    mass dependence estimated (2009)

    Schroeder, Steinhauser; Chetyrkin, Kuhn, Sturm
    Spira; Anastasiou, Bucherer, Kunszt
- Available fully differential code at NNLO
  - FeHiP/FehiPro, HNNLO
    Catani, Grazzini, Sargsyan
    Anastasiou, Melnikov, Petriello, Bucherer, Bucherer, Kunszt, Lazopoulos, Stoeckli

#### Intro: Drell-Yan Process

- Drell Yan process is crucial at hadron colliders
  - Detector Calibration
  - Luminosity Monitor
  - PDF Determination
  - New Physics Search
  - QCD and EW Study
- Very stable expansion in perturbative calculation
- Theoretical error below percent level



- qT resummation worked out using several different analytic methods and experimental data available for comparison
- Fully differential code at NNLO in QCD

Melnikov, Petriello, Gavin, YL,
• FEWZ, DYNNLO

Quackenbush

Catani, Cieri, Ferrera, De Florian, Grazzini,

# Prospect of NNLO



NNLO now a booming industry:

H+1jet, top pair, di-boson, ...

Loop calculation

Boughezal, Caola, Melnikov, Petriello, Schulze; Chen, Gehrmann, Glover, Jaquier Czakon, Fiedler, Mitov; Abelof, Gehrmann-De Ridder, Maierhoefer, Pozzorini Cascioli, Gehrmann, Grazzini, Kallweit, MaierHoefer, von Manteuffel, Pozzorini, Rathlev Tancredi, Torre, Weihs, Anastasiou, Duhr, Lazopoulos

Many known but multi-scale 2-loop integrals still a
 Gehrmann, Jaquier, Glover, Koukoutsakis, Tancredi, Weihs
 Henn, Melnikov, Smirnov

Phase space integration (IR regularization)

Catani, Grazzini

qT-subtraction method;
 Cut-off method by phase space slicing;
 Phase space partitioning and sector decomposition;
 Antenna subtraction.

Abelof, Bernreuther, Bogner, Dekkers, Gehrmann-De Ridder, etc.

### Questions

#### Why do NNLO ?

Quantitative predictive power only starts at NLO; need NNLO for high precision, especially for Higgs!

#### Why do Parton Shower?

Partonic level events not enough for detector simulation, need hadronic level events

### What is Parton Shower

Very complicated environment inside LHC

 Short distance physics obscured by long distance ones

Initial state radiation

Final state radiation

Hadronization

Multiple Parton Interaction

Simulated by PS

•

PS bridges theoretical calculation with detector simulation

# Enough?

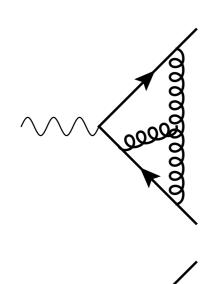
PS bridges theoretical calculation with detector simulation



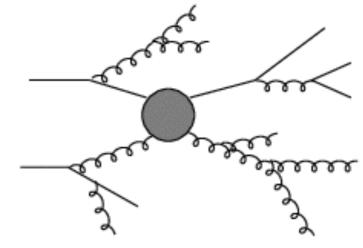


- Current way of interfacing NNLO is rather crude
  - Differential NNLO K-factor
- Intrinsic difficulty in combining NNLO with PS
  - Problem starts at NLO

# (N)NLO and Parton Shower

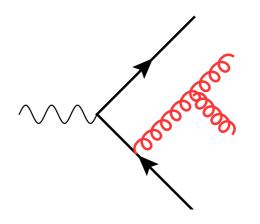






- Loops / Virtual:
  - IR divergent by itself ⇒
     cannot shower divergence





PS have 0 to ∞ emissions ⇒
 double counting

# (N)NLO and Parton Shower

- Problem 1: <u>IR divergence</u>
  - Fixed order has delicate cancellation between real and virtual
  - Parton shower eliminates divergence by resummation
- Problem 2: <u>double counting</u>
  - Fixed order adopts true ME
  - Parton shower ME is only approximate

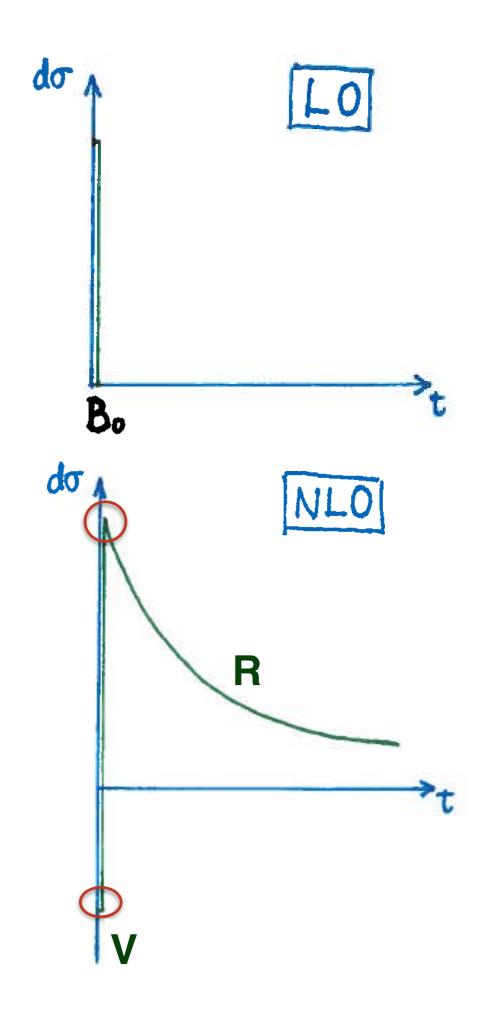
# IR singularity

- Real Emission ME is singular in IR limit
  - KLN theorem guarantees that IR sing. cancel between Real and Virtual

$$V \propto \left(\frac{1}{-\delta(t)}\right) \qquad \text{cancel !}$$
 
$$R \propto t^{-1-\epsilon} = \left(-\frac{1}{\epsilon}\delta(t) + [t^{-1-\epsilon}]_{+}\right)$$

plus distribution prescribes a sharp subtraction at t=0 to ensure finite inclusive result

$$\int dt \, [f(t)]_{+} g(t) = \int dt \, [f(t)]_{+} \, \{g(t) - g(0)\}$$



# IR singularity

- IR-finite only inclusively: R diverges as it approaches t=0
- A simple way to do differential NLO is to have a cut-off that's below observable limit
  - below cut-off: Combined with Virtual
  - above cut-off: IR-div. regulated by cut-off

$$R \propto t^{-1-\epsilon} = -\frac{1}{\epsilon} + [t^{-1-\epsilon}]_{+}$$

$$\xrightarrow{t_0 \to 0} -\frac{1}{\epsilon} + \log(t_0)\delta(t) + \frac{1}{t}\theta(t - t_0) + \mathcal{O}(\epsilon)$$

 $t_0$ 

logarithmic dependence on cut-off

# Logarithms

Observables like pT effectively introduce a cut-off

$$\Rightarrow L = \log(t_0)$$

- NLO: up to 1 emission
  - next-to-leading-logarithm (NLL)

$$\alpha_S(L^2,L)$$

- NNLO: up to 2 emissions
  - next-to-next-to-leading-logarithm (NNLL)

$$\alpha_S(L^2, L) + \alpha_S^2(L^4, L^3, L^2, L)$$

FO becomes unstable when L becomes large ⇒ resummation

# IR Singularity in Parton Shower

Parton shower takes a different approach

Singularity suppressed by Sudakov

V=-R=-K if neglecting IR-finite 
$$V \to e^V - 1 \xrightarrow{\text{terms}} e^{-K} - 1$$
 
$$R \to e^{-K} K$$

**Sudakov Form Factor** 

 $\lim_{t \to 0} e^{-1/t} \frac{1}{t} \to 0$ do exp(-K) -Ma

K is approximately R; approaching R in IR limit

In the IR limit, the ME takes a factorized form

$$|\mathcal{M}_{n+1}|^2 \sim K_n |\mathcal{M}_n|^2$$

$$|\mathcal{M}_n|^2$$

$$|\mathcal{M}_n|^2$$

Multiple emissions are approximated by iterating the

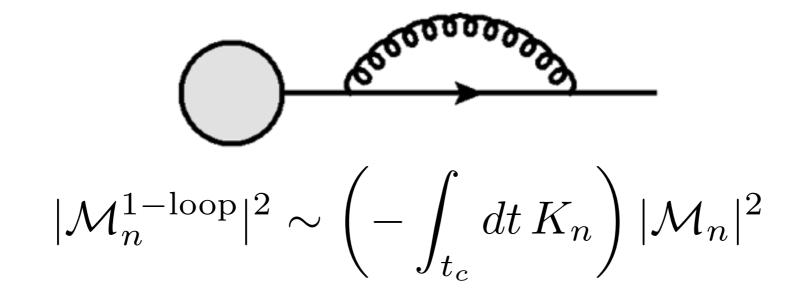
above formula

minating scale egularte IR div. 
$$1 + \int_{t_c}^{\mu_Q^2} dt \, K_n + \int_{t_c}^{\mu_Q^2} dt \, K_n \int_{t_c}^t dt \, K_{n+1} + \int_{t_c}^{t_Q} dt \, K_n \int_{t_c}^t dt' \, K_{n+1} \int_{t_c}^{t'} dt'' \, K_{n+2} + \dots$$

hard scale to start PS

terminating scale to regularte IR div.

Approximate Virtual by integrated Real



- A "failed" attempt to emit
- Iterated Virtual gives Sudakov form factor  $e^{-K}$

$$\Pi_n(t_c, \mu_Q^2) = \exp\left\{-\int_{t_c}^{\mu_Q^2} dt \, K_n\right\} = 1 - \int_{t_c}^{\mu_Q^2} dt \, K_n(t) \Pi_n(t, \mu_Q^2)$$

$$\begin{split} &\Pi_n(t_c,\mu_Q^2) = \exp\left\{-\int_{t_c}^{\mu_Q^2} dt\,K_n\right\} = 1 - \int_{t_c}^{\mu_Q^2} \frac{\text{failed emission @ t}}{dt\,K_n(t)} \frac{1}{\Pi_n(t,\mu_Q^2)} \\ &\text{no emission probability} \\ &\xrightarrow{\mu_Q^2} \qquad t_c = \frac{1 - \int_{t_c}^{\mu_Q^2} \frac{\text{failed emission @ t}}{dt\,K_n(t)} \frac{1}{\Pi_n(t,\mu_Q^2)} \\ &\xrightarrow{\mu_Q^2} \qquad t_c = \frac{1 - \int_{t_c}^{\mu_Q^2} \frac{\text{failed emission @ t}}{dt\,K_n(t)} \frac{1}{\Pi_n(t,\mu_Q^2)} \\ &\xrightarrow{\mu_Q^2} \qquad t_c = \frac{1 - \int_{t_c}^{\mu_Q^2} \frac{\text{failed emission @ t}}{dt\,K_n(t)} \frac{1}{\Pi_n(t,\mu_Q^2)} \\ &\xrightarrow{\mu_Q^2} \qquad t_c = \frac{1 - \int_{t_c}^{\mu_Q^2} \frac{\text{failed emission @ t}}{dt\,K_n(t)} \frac{1}{\Pi_n(t,\mu_Q^2)} \\ &\xrightarrow{\mu_Q^2} \qquad t_c = \frac{1 - \int_{t_c}^{\mu_Q^2} \frac{\text{failed emission @ t}}{dt\,K_n(t)} \frac{1}{\Pi_n(t,\mu_Q^2)} \\ &\xrightarrow{\mu_Q^2} \qquad t_c = \frac{1 - \int_{t_c}^{\mu_Q^2} \frac{\text{failed emission @ t}}{dt\,K_n(t)} \frac{1}{\Pi_n(t,\mu_Q^2)} \\ &\xrightarrow{\mu_Q^2} \qquad t_c = \frac{1 - \int_{t_c}^{\mu_Q^2} \frac{\text{failed emission @ t}}{dt\,K_n(t)} \frac{1}{\Pi_n(t,\mu_Q^2)} \\ &\xrightarrow{\mu_Q^2} \qquad t_c = \frac{1 - \int_{t_c}^{\mu_Q^2} \frac{\text{failed emission @ t}}{dt\,K_n(t)} \frac{1}{\Pi_n(t,\mu_Q^2)} \\ &\xrightarrow{\mu_Q^2} \qquad t_c = \frac{1 - \int_{t_c}^{\mu_Q^2} \frac{\text{failed emission @ t}}{dt\,K_n(t)} \frac{1}{\Pi_n(t,\mu_Q^2)} \\ &\xrightarrow{\mu_Q^2} \qquad t_c = \frac{1 - \int_{t_c}^{\mu_Q^2} \frac{\text{failed emission @ t}}{dt\,K_n(t)} \frac{1}{\Pi_n(t,\mu_Q^2)} \\ &\xrightarrow{\mu_Q^2} \qquad t_c = \frac{1 - \int_{t_c}^{\mu_Q^2} \frac{\text{failed emission @ t}}{dt\,K_n(t)} \frac{1}{\Pi_n(t,\mu_Q^2)} \\ &\xrightarrow{\mu_Q^2} \qquad t_c = \frac{1 - \int_{t_c}^{\mu_Q^2} \frac{\text{failed emission @ t}}{dt\,K_n(t)} \frac{1}{\Pi_n(t,\mu_Q^2)} \\ &\xrightarrow{\mu_Q^2} \qquad t_c = \frac{1 - \int_{t_c}^{\mu_Q^2} \frac{\text{failed emission @ t}}{dt\,K_n(t)} \frac{1}{\Pi_n(t,\mu_Q^2)} \\ &\xrightarrow{\mu_Q^2} \qquad t_c = \frac{1 - \int_{t_c}^{\mu_Q^2} \frac{\text{failed emission @ t}}{dt\,K_n(t)} \frac{1}{\Pi_n(t,\mu_Q^2)} \\ &\xrightarrow{\mu_Q^2} \qquad t_c = \frac{1 - \int_{t_c}^{\mu_Q^2} \frac{\text{failed emission @ t}}{dt\,K_n(t)} \frac{1}{\Pi_n(t,\mu_Q^2)} \\ &\xrightarrow{\mu_Q^2} \qquad t_c = \frac{1 - \int_{t_c}^{\mu_Q^2} \frac{\text{failed emission @ t}}{dt\,K_n(t)} \frac{1}{\Pi_n(t,\mu_Q^2)} \\ &\xrightarrow{\mu_Q^2} \qquad t_c = \frac{1 - \int_{t_c}^{\mu_Q^2} \frac{\text{failed emission @ t}}{dt\,K_n(t)} \frac{1}{\Pi_n(t,\mu_Q^2)} \\ &\xrightarrow{\mu_Q^2} \qquad t_c = \frac{1 - \int_{t_c}^{\mu_Q^2} \frac{\text{failed emission @ t}}{dt\,K_n(t)} \frac{1}{\Pi_n(t,\mu_Q^2)} \\ &\xrightarrow{\mu_Q^2} \qquad t_c = \frac{1 - \int_{t_c}^{\mu_Q^2} \frac{\text{failed emission @ t}}{dt\,K_n(t)} \frac{1}{\Pi_n(t,\mu_Q^2)} \\ &\xrightarrow{\mu_Q^2} \qquad t_c = \frac{1 -$$

Sudakov calculates zero emission probability in PS evolution

Rewrite: 
$$1 = \Pi_n(t_c, \mu_Q^2) + \int_{t_c}^{\mu_Q^2} dt \, K_n(t) \Pi_n(t, \mu_Q^2)$$

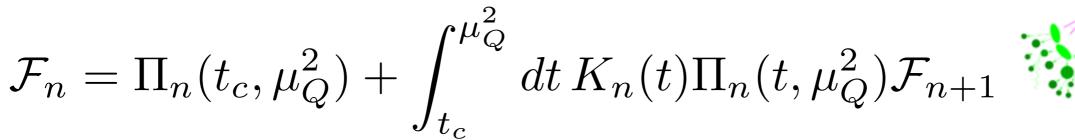
Reinterpret:

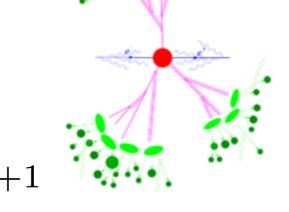
no emission at all 
$$1 = \Pi_n(t_c, \mu_Q^2) + \int_{t_c}^{\mu_Q^2} \frac{1 \text{ emission @ t}}{dt \ K_n(t) \Pi_n(t, \mu_Q^2)}$$
 no emission till t 
$$= \frac{1}{\mu_Q^2} + \frac{1}{\mu_Q^2}$$

PS respects unitarity
 Virtual cancels Real perfectly ⇒ inclusive rate unchanged !

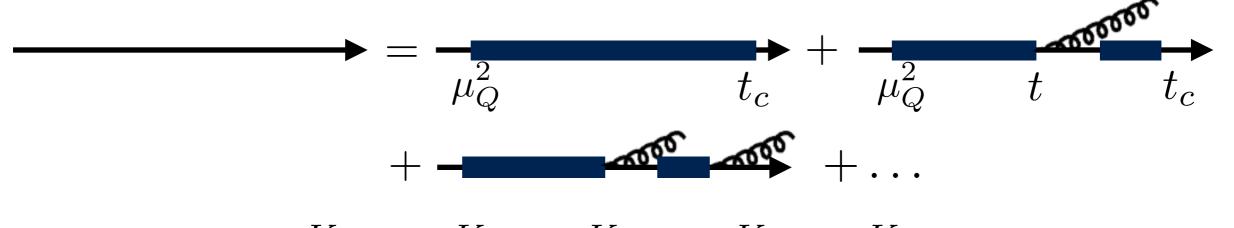
PS Generating Function  $\mathcal{F}_n = \Pi_n(t_c,\mu_Q^2) + \int_{t_c}^{\mu_Q^2} dt \, K_n(t) \Pi_n(t,\mu_Q^2) \underline{\mathcal{F}_{n+1}}$  recursive def.

# Parton Shower





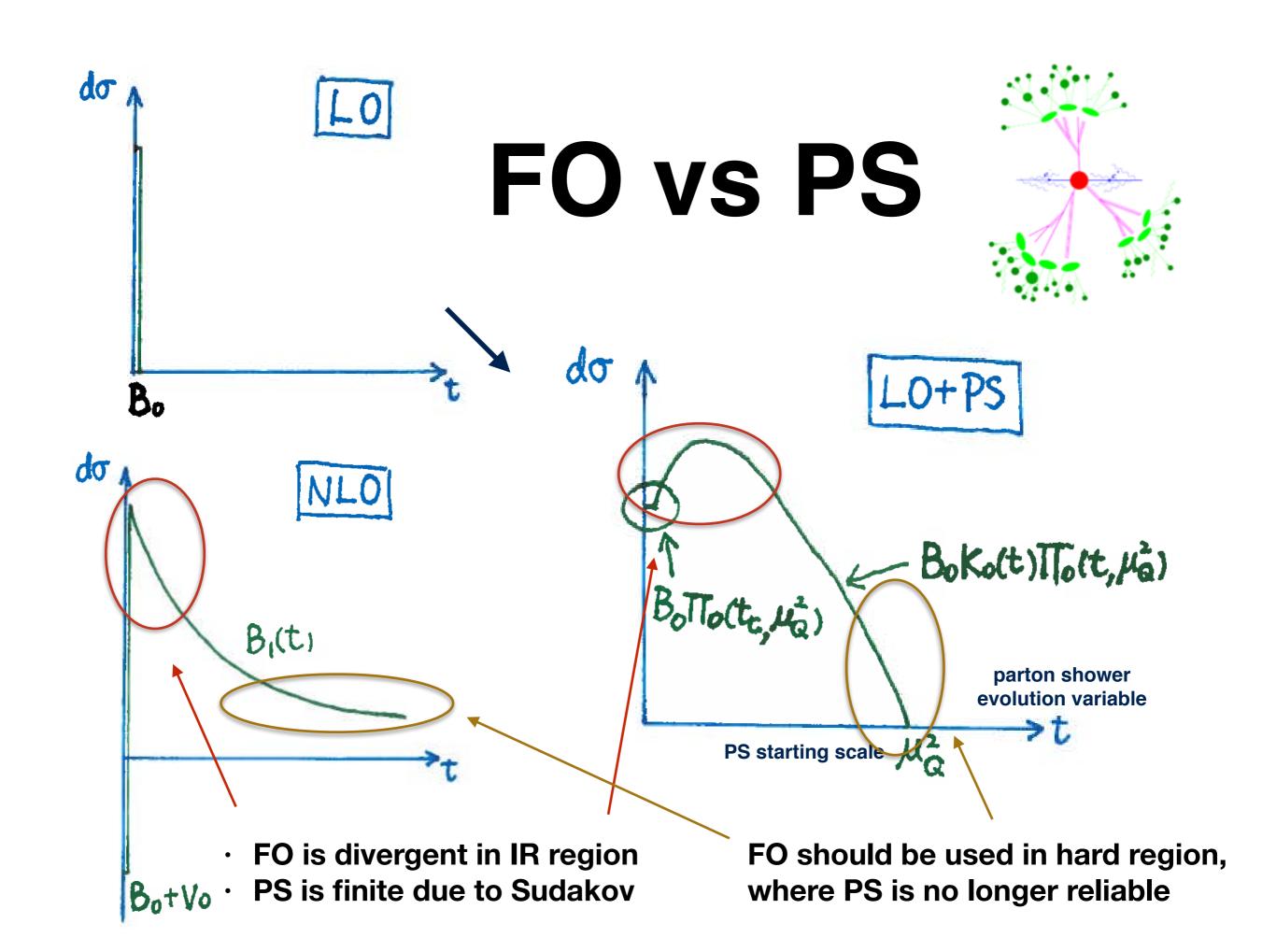
Iterated for more emissions



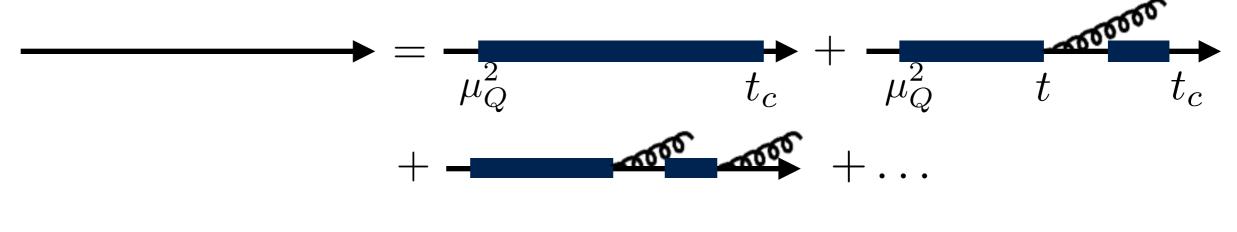
$$1 = e^{-K} + e^{-K}Ke^{-K} + e^{-K}Ke^{-K}K + \dots$$

Infinite emissions: automatic resummation
iterated (ordered) single emissions ⇒ approx. NLL accurate

$$\exp\{\alpha_S(L^2,L)\}$$



## Fix?



$$1 = e^{-K} + e^{-K}Ke^{-K} + e^{-K}Ke^{-K}K + \dots$$

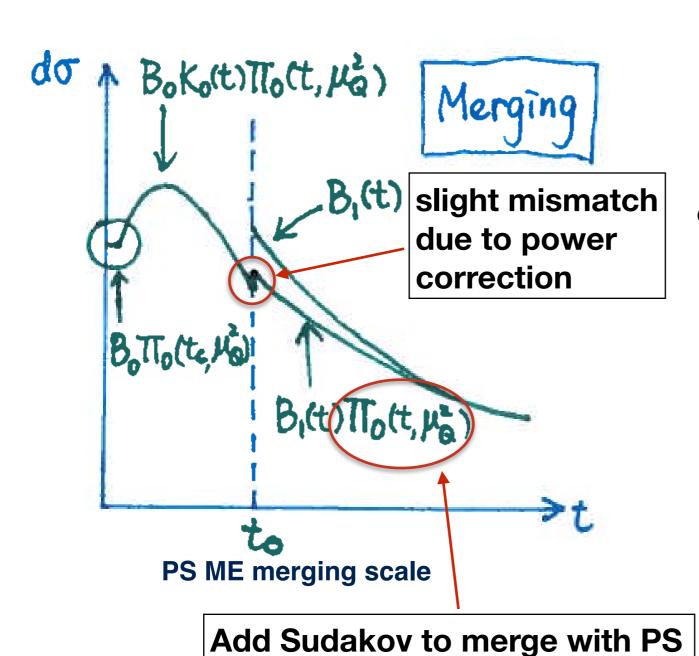
Each emission can be corrected by actual MEs

$$e^{-K}K \rightarrow e^{-K}\left(K|_{t < t_0} + R|_{t > t_0}\right)$$
 merging scale

- Add ME correction in hard region
- Keep PS in IR region
- Use merging scales to separate two regions

### "Fix the PS"

$$e^{-K} + e^{-K}K \to e^{-K} + e^{-K}(K|_{t < t_0} + R|_{t > t_0})$$



 mismatch is IR-finite and vanishes when merging scale becomes small

$$R - K \xrightarrow{t \to 0} 0$$

 Hard region restored at the expense of unitarity (extra Sudakov fades away)

$$e^{-K}R = \exp\{-\int_{t}^{\mu^{2}} dt' K(t')\} R(t)$$

$$\xrightarrow{t \to \mu^{2}} R$$

Merging scale dependence

# Merging

$$e^{-K} + e^{-K}K \to e^{-K} + e^{-K}(K|_{t < t_0} + R|_{t > t_0})$$

- Merging of MEs:
   ME correction for each jet multiplicity in PS
  - merging scale dependence dominated by subleading logarithmic terms

IR limit of many emission ME not fully captured by PS

· Examples:

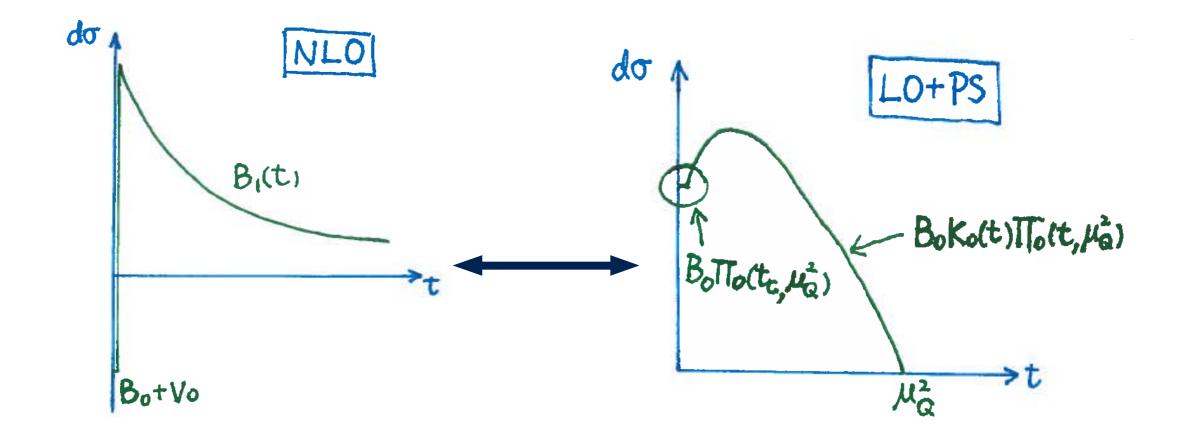
MLM, CKKW, CKKW-L, Truncated Shower, Pseudo-shower

Catani, Hoeche, Krauss, Kuhn, Lonnblad, Mangano, Mrenna, Richardson, Schumann, Siegert, Webber, ...

# Matching



- Would also like to have higher order inclusive accuracy
  - correct emission pattern in hard region × (merging)
  - keep PS resummation in IR region × (merging)
  - correct FO inclusive rate



# Matching @ NLO

- Apply NLO differential K-factor ?
  - PS starts with a single topology
     All shower emissions have a parent Born topology
  - LO has only Born topology for H/W/Z production, the final state is exclusively H/W/Z
  - NLO contains emission ME for H/W/Z production, there is final state of H/W/Z + 1 jet

Combining two multiplicities is addressed by merging but didn't do it "right"

# Matching @ NLO

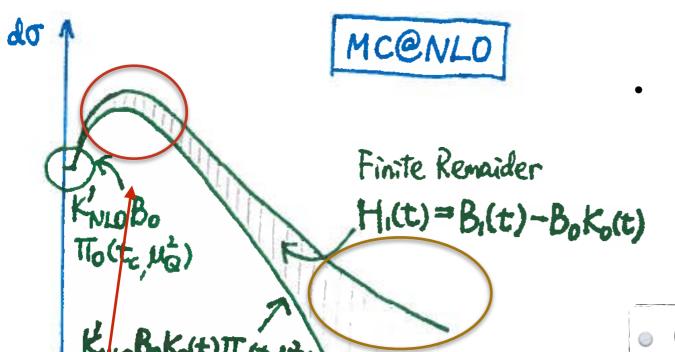
For simplicity take Born B=1

NLO: 
$$1 + V + R = (1 + V + K) + (R - K)$$
PS:  $e^{-K} + e^{-K}K$ 
finite
NLO  $\otimes$  PS:  $(1 + V + K)(e^{-K} + e^{-K}K) + (R - K)$ 

- Use PS "K" as a subtraction term
  - Integrated to cancel IR div. in Virtual can be mapped to Born ⇒ (approx.) NLO K-factor
  - Keep differential to cancel IR div. in Real R-K difference is non-singular  $\Rightarrow$  hard remainder
    - PS makes up the "K" part: no double counting

# Matching @ NLO

$$(1 + V + K)(e^{-K} + e^{-K}K) + (R - K)$$



Widely used approaches: MC@NLO, POWHEG

Frixione, Webber, Nason, Oleari

- POWHEG takes K=R
- Correct emission pattern in hard region ×
- Keep PS resummation in IR region ×
- Correct NLO inclusive rate ×

dominated by PS 
$$k'_{\rm NLO}e^{-K}K + (R-K)$$

 $R \to K$ 

$$\rightarrow k'_{\rm NLO} e^{-K} K$$

$$e^{-K} \rightarrow 1$$
 full ME restored

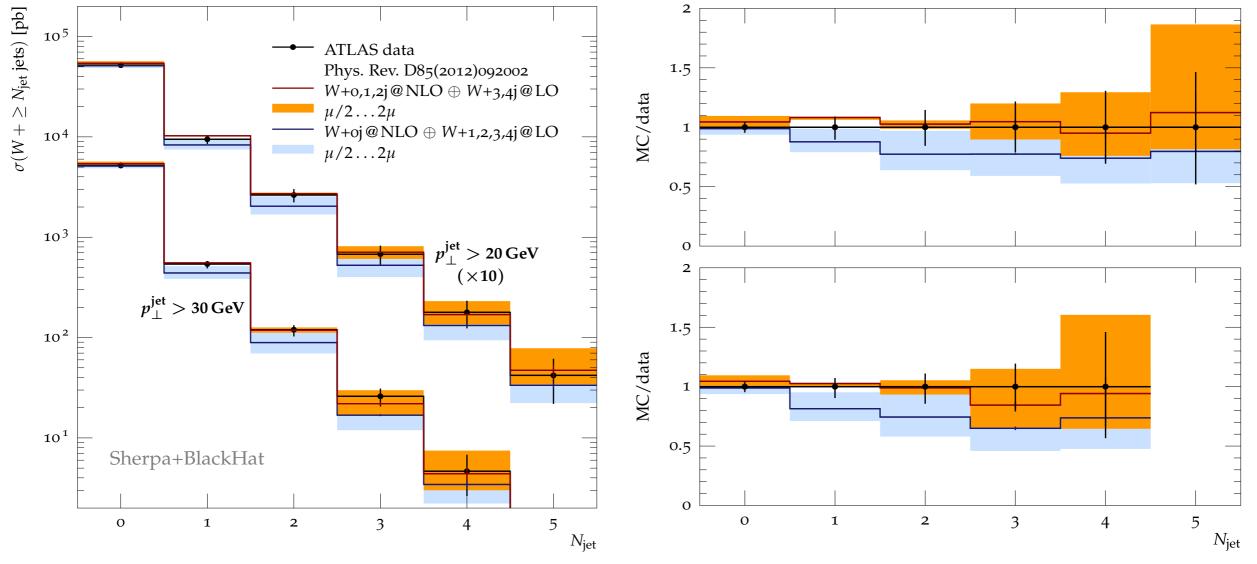
$$k'_{\rm NLO}e^{-K}K + (R - K) \to R + \mathcal{O}(\alpha_S)$$

# Merged Matching

- PS matched NLO can also be merged:

  Gehrmann, Hoeche, Krauss, Schoenherr, Siegert ...

  Gehrmann, Hoeche, Krauss, Schoenherr, Siegert ...
  - Example: W + n jets merged in Sherpa



Hoeche, Krauss, Schoenherr, Siegert arXiv:1207.5030

#### **Extension to NNLO?**

$$(1+V+K)(e^{-K}+e^{-K}K)+(R-K)$$

Require flexible subtraction method of NNLO
 flexible enough to be used in the PS "K" for numerical Sudakov

Hamilton, Nason, Zanderighi, Re

- MINLOS overcome the difficulty by using analytic Sudakov
  - process-specific
  - possible mismatch with Sudakov in subsequent PS
  - requires extra input of differential NNLO K-factor
- Is there another way to combine FO with PS?
   can we improve the merging procedure to achieve higher order accuracy?

# Unitarized Merging

First restore unitarity for merging

Lonnblad, Prestel

modified Real ⇒ no more perfect cancellation btw Real and Virtual

$$e^{-K} + e^{-K}K) \rightarrow e^{-K} + e^{-K}(K|_{t < t_0} + R|_{t > t_0}) \text{ emission}$$

 Unitarized merging corrects Sudakov order by order to restore the cancellation

$$= \frac{1}{\mu_Q^2} + \frac{1}{\mu_Q^2}$$

#### UNLOPS

Hoeche, Lonnblad, Prestel, YL

Obtain NLO inclusive rate by adding additional terms

">" refers to 
$$t > t_0$$

" < " refers to 
$$t < t_0$$

$$e^{-K} + e^{-K}K \to 1 - e^{-K}(K_{<} + R_{>}) + e^{-K}(K_{<} + R_{>})$$

$$\xrightarrow{\text{add NLO}} 1 + V + R - e^{-K}(K_{<} + R_{>}) + e^{-K}(K_{<} + R_{>})$$

take merging scale to be as small as PS terminating scale

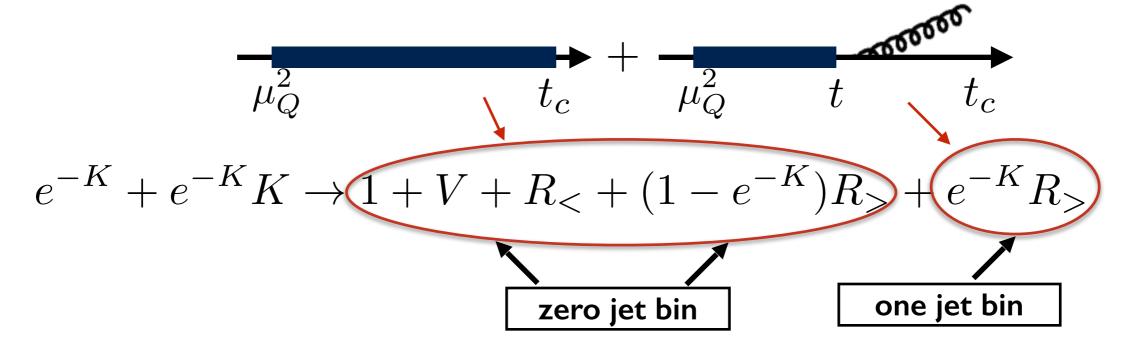
$$t_0 \to t_c \sim 0 \Rightarrow \operatorname{drop} K_{<}$$

separate Real by the terminating/merging scale

$$R = R_{<} + R_{>}$$

**Phase Space** Slicing

#### **UNLOPS**



- Correct emission pattern in hard region  $\times e^{-K}R_{>} \to R$
- Keep PS resummation in IR region  $\times$   $e^{-K}R_{>} \rightarrow e^{-K}K$
- Correct NLO inclusive rate  $\times$   $\equiv 1 + V + R$

 $(1 - e^{-K})R_{>}$  obtained by probability conservation from  $e^{-K}R_{>}$ 

- Subsequent PS continues in the one jet bin
- · Close related to the phase space slicing method

# UNLOPS vs. MC@NLO/POWHEG

MC@NLO/POWHEG: 
$$(1 + V + K)(e^{-K} + e^{-K}K) + (R - K)$$
  
UNLOPS:  $1 + V + R_{<} + (1 - e^{-K})R_{>} + e^{-K}R_{>}$ 

- Matching (MC@NLO/POWHEG)
  - multiplicative (V is showered)
  - · closely related to the subtraction method

$$1 + V + R = (1 + V + K) + (R - K)$$

- Merging (UNLOPS)
  - additive (V is not showered)
  - · closely related to the phase space slicing method

$$1 + V + R = (1 + V + R_{<}) + R_{>}$$

higher order effect ⇒

regarded as theoretical uncertainty

#### **Extension to NNLO?**

$$MC@NLO/POWHEG: (1 + V + K)(e^{-K} + e^{-K}K) + (R - K)$$

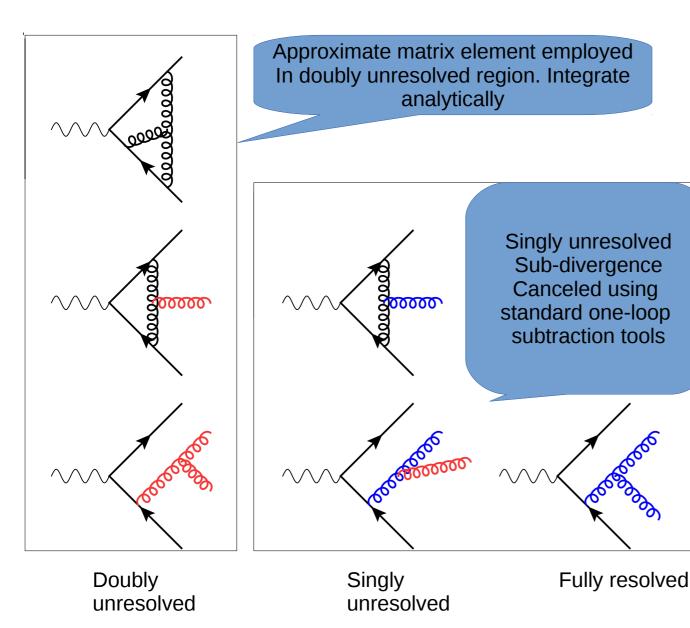
- No generic extension
  - Currently no flexible subtraction method of NNLO

UNLOPS: 
$$1 + V + R_{<} + (1 - e^{-K})R_{>} + e^{-K}R_{>}$$

- · Straightforward generic extension
  - first need NNLO calculation with phase space slicing

## Sherpa NNLO

Catani, Grazzini



- qT < qT cut-off jet-vetoed NNLO
- qT > qT cut-off H/W/Z + 1jet @ NLO

- Phase space sliding method by H/W/Z qT (based on qT subtraction by Catani and Grazzini)
  - Above the cut-off: H/W/Z + 1jet @ NLO
  - Below the cut-off: Jetvetoed NNLO
    - Well approximated by prediction from factorization theorem

```
small qT cut-off ⇒
large cancellation ⇒
possible numerical instability
```

contains 2-loop virtual and IR limit of double real emission



## Sherpa NNLO

- Sherpa now has H/W/Z production at NNLO
- · full event generation
- · interface with Rivet

• • •

- · (Relatively) Easy to do
  - Sherpa already has W/Z/H+1jet at NLO from Blackhat and internal implementation - very stable

Berger, Bern, Dixon, etc.

Ravindran, Smith, van Neerven

- Below qT cut-off obtained from existing SCET results
   well established
- Also combined with PS
  - Use the method of UN2LOPS

### **UNLOPS to UN2LOPS**

UNLOPS:  $1 + V + R + (1 - e^{-K})R + (e^{-K})R > 0$ 

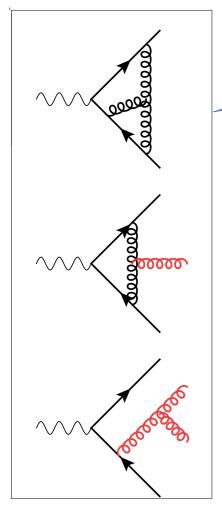
qT < qT cut-off Jet-vetoed NNLO Born kinematics

qT > qT cut-off

NLO H/W/Z + 1jet

handled by MC@NLO

Residual IR divergence suppressed - incomplete PS is only approx. NLL NNLO contains NNLL

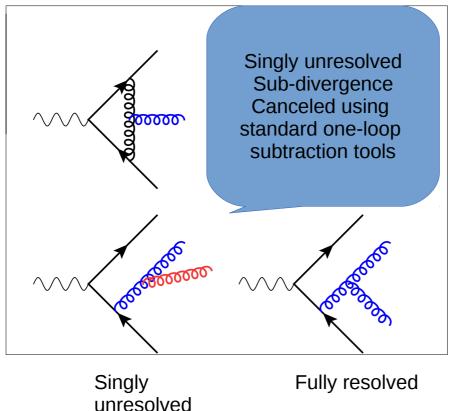


Doubly

unresolved

Approximate matrix element employed In doubly unresolved region. Integrate analytically

- UN2LOPS
   H/W/Z: NNLO inclu. accurate
  - H/W/Z + 1 jet: NLO inclu. accurate
  - H/W/Z + 2 jets: LO accurate
  - H/W/Z + >2 jets: PS accurate
  - H/W/Z + soft jets: most logs resummed (limited by PS accuracy)



### Final Formula

$$\begin{split} \langle O \rangle &= \int \mathrm{d}\Phi_0 \, \bar{\bar{\mathbb{B}}}_0^{t_c} \, O(\Phi_0) \\ &+ \int_{t_c} \mathrm{d}\Phi_1 \, \Big[ 1 - \Pi_0(t_1, \mu_Q^2) \, \Big( w_1 + w_1^{(1)} + \Pi_0^{(1)}(t_1, \mu_Q^2) \Big) \Big] \, \mathrm{B}_1 \, O(\Phi_0) \\ &+ \int_{t_c} \mathrm{d}\Phi_1 \, \Pi_0(t_1, \mu_Q^2) \Big( w_1 + w_1^{(1)} + \Pi_0^{(1)}(t_1, \mu_Q^2) \Big) \, \mathrm{B}_1 \, \bar{\mathcal{F}}_1(t_1, O) \\ &+ \int_{t_c} \mathrm{d}\Phi_1 \, \Big[ 1 - \Pi_0(t_1, \mu_Q^2) \Big] \, \tilde{\mathrm{B}}_1^{\mathrm{R}} \, O(\Phi_0) + \int_{t_c} \mathrm{d}\Phi_1 \, \Pi_0(t_1, \mu_Q^2) \, \tilde{\mathrm{B}}_1^{\mathrm{R}} \, \bar{\mathcal{F}}_1(t_1, O) \\ &+ \int_{t_c} \mathrm{d}\Phi_2 \, \Big[ 1 - \Pi_0(t_1, \mu_Q^2) \Big] \, \mathrm{H}_1^{\mathrm{R}} \, O(\Phi_0) + \int_{t_c} \mathrm{d}\Phi_2 \, \Pi_0(t_1, \mu_Q^2) \, \mathrm{H}_1^{\mathrm{R}} \, \mathcal{F}_2(t_2, O) \\ &+ \int_{t_c} \mathrm{d}\Phi_2 \, \, \mathrm{H}_1^{\mathrm{E}} \, \mathcal{F}_2(t_2, O) \end{split}$$

Tree level amplitude and subtraction from Amegic or Comix

[Krauss, Kuhn, Soff] hep-ph/0109036, [Gleisberg, Krauss] arXiv:0709.2881, [Gleisberg, Hoeche] arXiv:0808.3674

One loop virtual matrix element from Blackhat, or internal Sherpa

[Berger et al.] arXiv:0803.4180, [Berger et al.] arXiv:0907.1984 arXiv:1004.1659 arXiv:1009.2338

NNLO vetoed cross section using recent SCET results

[Becher, Neubert] arXiv:1007.4005 arXiv:1212.2621, [Gehrmann, Luebbert, Yang] arXiv:1209.0682 arXiv:1403.6451 arXiv:1401.1222

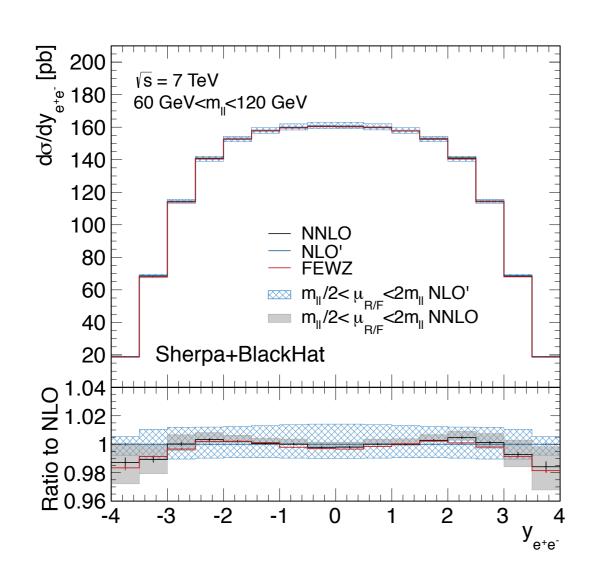
Parton shower based on Catani-Seymour dipole

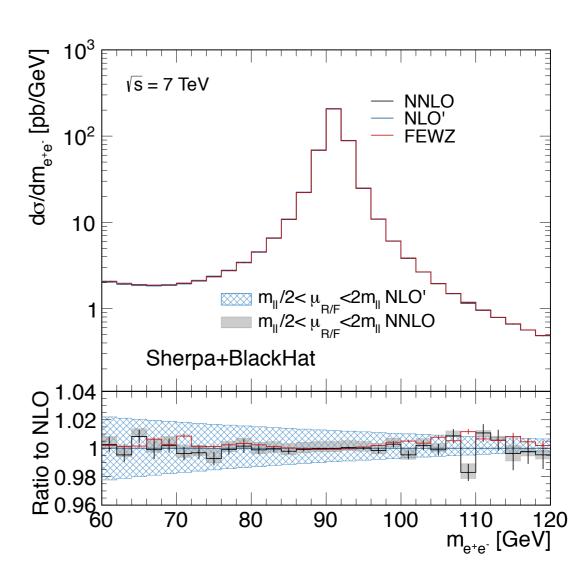
[Schumann, Krauss] arXiv:0709.1027

Combined in Sherpa event generation framework

[Gleisberg et al.] hep-ph/0311263 arXiv:0811.4622

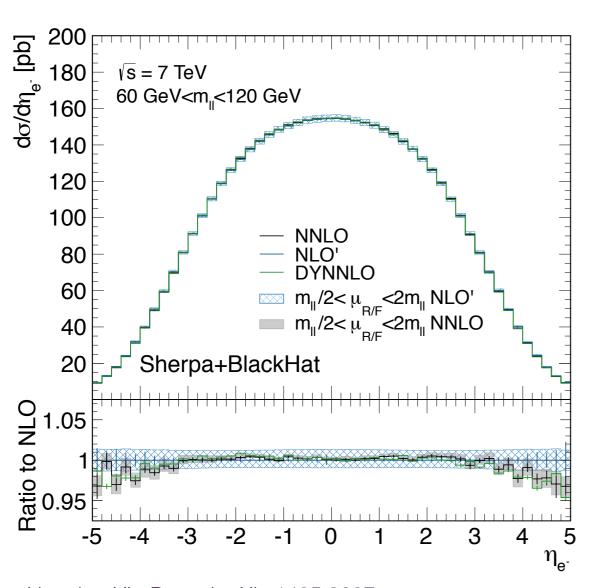
# DY: Validation with FEWZ and VRAP

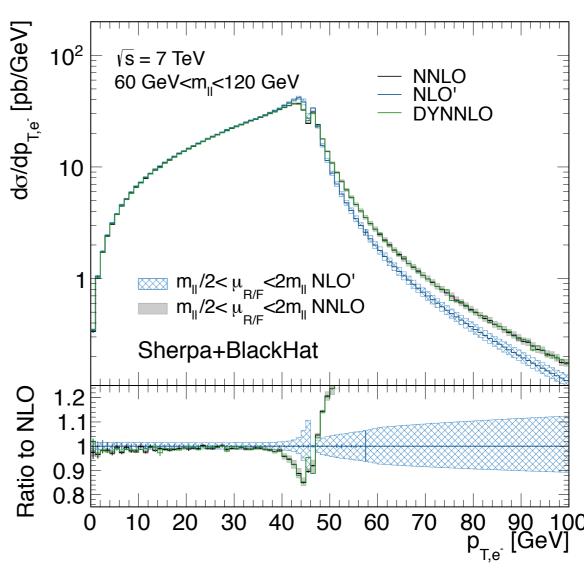




$E_{ m cms}$	7 TeV	14 TeV	33 TeV	100 TeV
VRAP	$973.99(9)^{+4.70}_{-1.84}$ pb	$2079.0(3) \begin{array}{c} +14.7 \\ -6.9 \end{array}$ pb	4909.7(8) $^{+45.1}_{-27.2}$ pb	$13346(3) \begin{array}{c} +129 \\ -111 \end{array}$ pb
SHERPA	$973.7(3) \begin{array}{l} +4.78 \\ -2.21 \end{array}$ pb	$2078.2(10)^{+15.0}_{-8.0}$ pb	$4905.9(28)^{+45.1}_{-27.9}$ pb	$13340(14)^{+152}_{-110}$ pb

# DY: Validation with DYNNLO

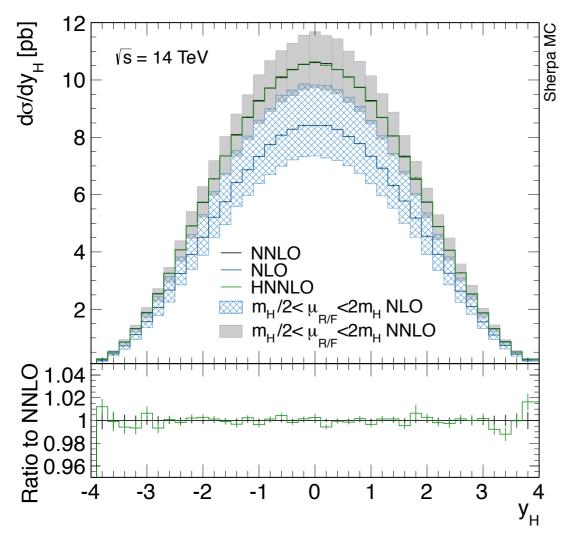


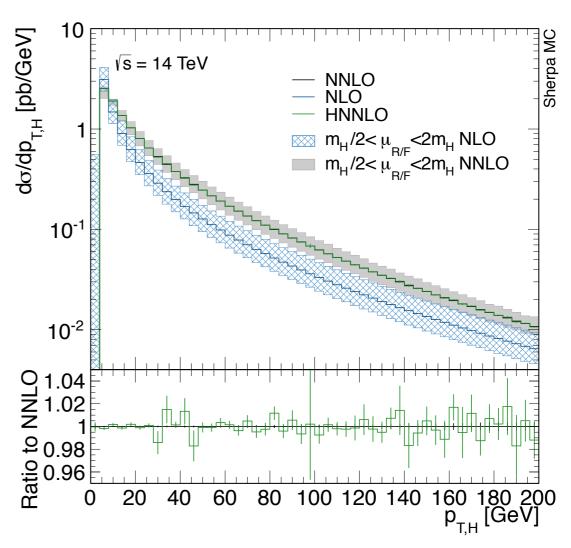


Hoeche, YL, Prestel arXiv:1405.3607

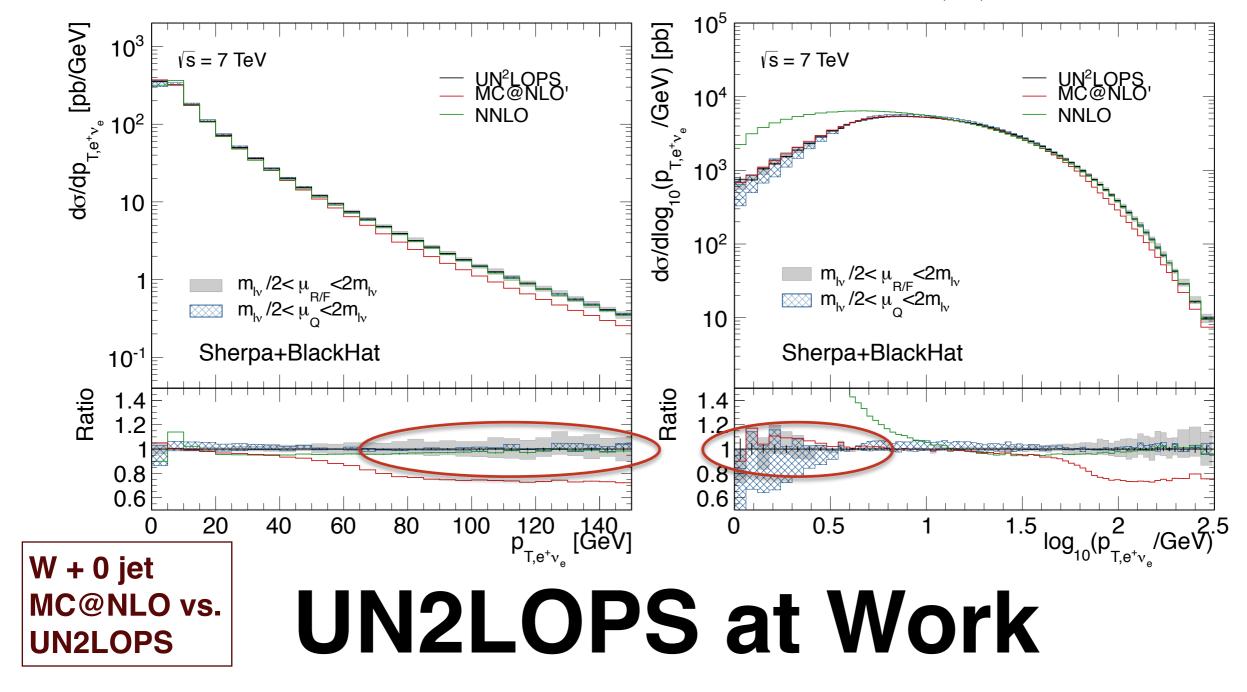
# Higgs: Validation with HNNLO

Hoeche, YL, Prestel, arXiv:1407.3773



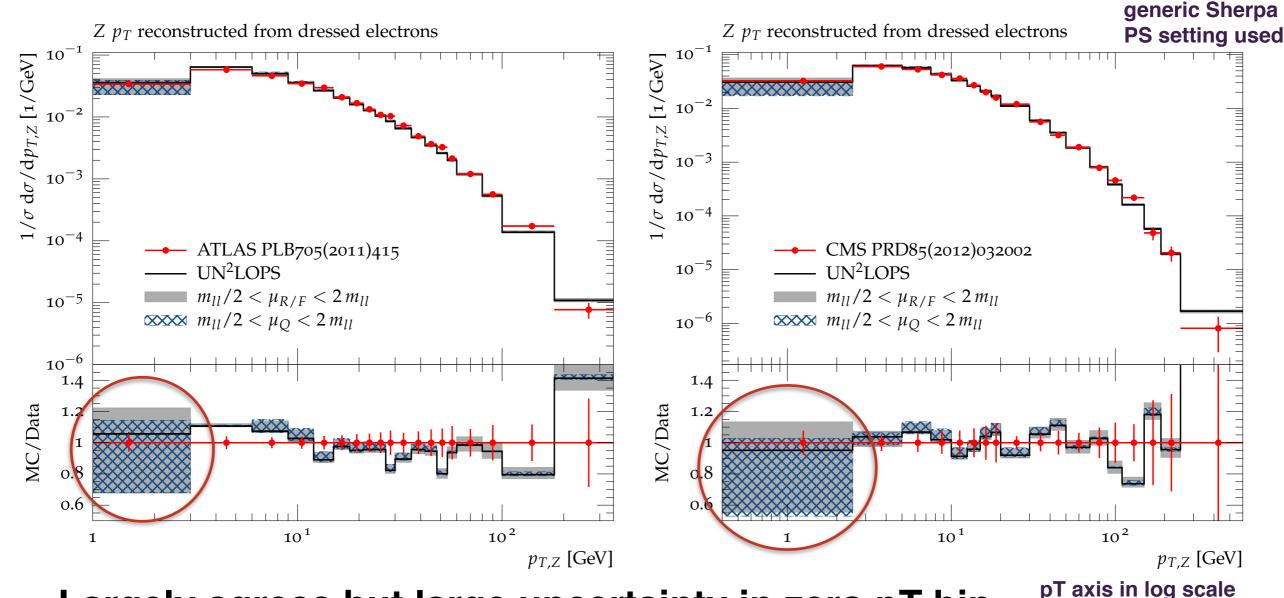


$E_{ m cms}$	7 TeV	14 TeV	33 TeV	100 TeV
HNNLO	$13.494(7)_{-1.382}^{+1.436} \text{ pb}$	$44.550(16)_{-3.954}^{+4.293} \text{ pb}$	$160.84(13)^{+13.29}_{-12.36} \text{ pb}$	_
SHERPA	$13.515(7)_{-1.382}^{+1.443} \text{ pb}$	$44.559(36)^{+4.226}_{-3.929}$ pb	$160.39(17)^{+13.47}_{-11.88} \text{ pb}$	$670.1(10)^{+47.9}_{-39.4} \text{ pb}$



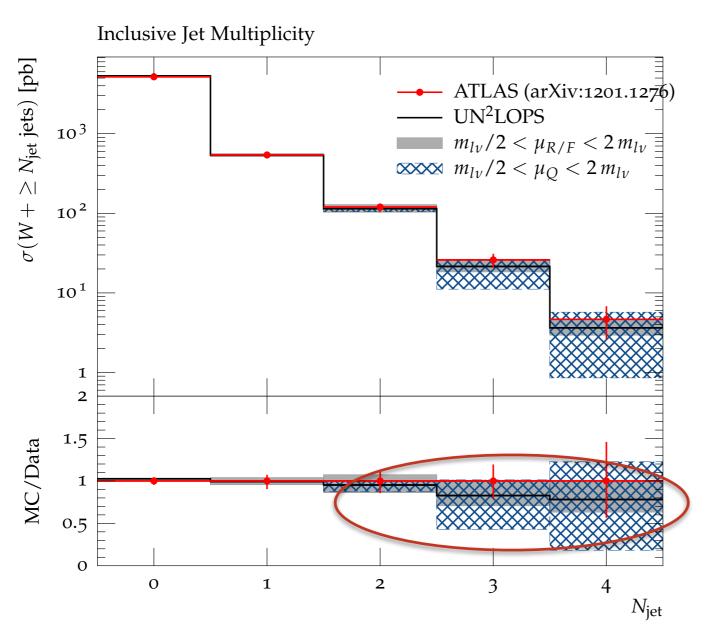
- UN2LOPS trumps both MC@NLO for H/W/Z + 0 and 1 jet
  - Good agreement with W+0jet at low pT, and becomes W+1jet at high pT
  - Also correct inclusive NNLO rate W+0jet

# Comparison with Exp.



- Largely agrees but large uncertainty in zero pT bin
  - Due to unresummed subleading logs of NNLO calculation
  - Scale variations of all finite pT bins propagate to zero pT bin by PS unitarity

## Comparison with Exp.



- UN2LOPS acts on 0, 1 and 2 jet bin:
  - Excellent agreement
  - Reduced uncertainty
- Improvement by merging with W + 2,3,4 jets @ NLO
  - Further reduced uncertainty

### UN2LOPS with Higgs

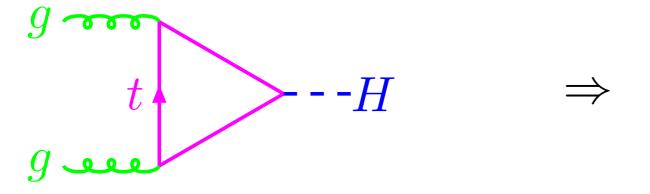
- The Application to Higgs: slight complication involved
  - Higgs NNLO is only worked out in EFT framework in massive top limit

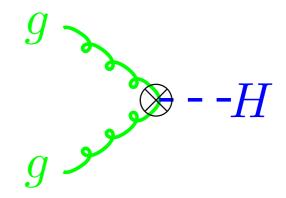
"SM Higgs NNLO" 
$$= H_g \times$$
 "EFT Higgs NNLO"

· Square of H-g-g effective coupling

generic NNLO

$$H_g = |c_g|^2 = h^{(0)} + \frac{\alpha_S}{4\pi}h^{(1)} + \left(\frac{\alpha_S}{4\pi}\right)^2 h^{(2)} + \dots$$





## UN2LOPS with Higgs

In FO, product is expanded and truncated in as ⇒
 "individual" matching

 $h^{(0)}$  is multiplied by generic Higgs NNLO matched with U2LOPS  $h^{(1)}$  is multiplied by generic Higgs NLO matched with MC@NLO  $h^{(2)}$  is multiplied by generic Higgs LO with simple parton shower

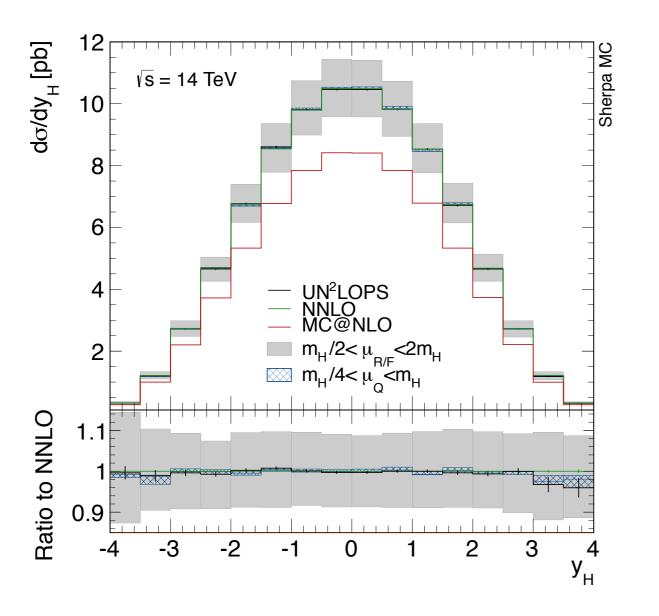
PS is all about factorization ⇒ "factorized" matching

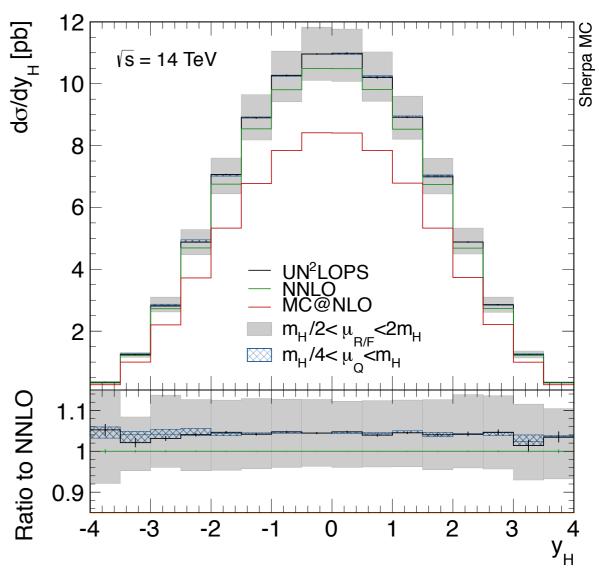
full  $H_g$  is multiplied by generic Higgs NNLO matched with U2LOPS

At 14TeV LHC, compared to "individual", "factorized" matching adds 14% w.r.t. Higgs LO 5% w.r.t. Higgs NNLO because large Higgs NLO is further enhanced by HO terms of Hg

# Higgs Rapidity

Hoeche, YL, Prestel arXiv:1407.3773





- left: "individual" matching; right: "factorized" matching
- Big improvement over MC@NLO
- Higgs rapidity spectrum unaffected by PS

### Outlook

- Provides experimental analysis with best theoretical accuracy at event out level
  - Straightforward to include finite top mass effect in UN2LOPS for Higgs
  - Same is true to include EW effects for both Higgs and DY processes
- UN2LOPS is a general framework
  - All differential NNLO calculation can be interfaced with given a suitable cut-off/merging parameter
  - Further improvement relies on an improved parton shower

### Outlook

 For well studied processes like Higgs and DY, an improved parton shower could be implemented based on analytic resummation

essentially adding ad-hoc terms to the parton shower kernels in order to reproduce the Sudakov form factor accurate to NNLL work in progress

- Pros
   All NNLO divergences are within control
   Uncertainty of parton shower is reduced
- Cons
   Sudakov from analytic resummation is process-specific and observable-dependent

## Summary

- First practical implementation of NNLO+PS for DY processes, also applied to Higgs production
  - Truly accessible NNLO for experimental analysis
  - Improved precision for Higgs and BSM study
  - Reduced uncertainty in traditional PS
- Flexible implementation, thanks to the Sherpa framework
  - Event generation at both NNLO and NNLO+PS
  - Interface with analysis tools such as Rivet available
  - Plugin to Sherpa (provided upon request)
- Parton shower improvement desirable for better overall accuracy

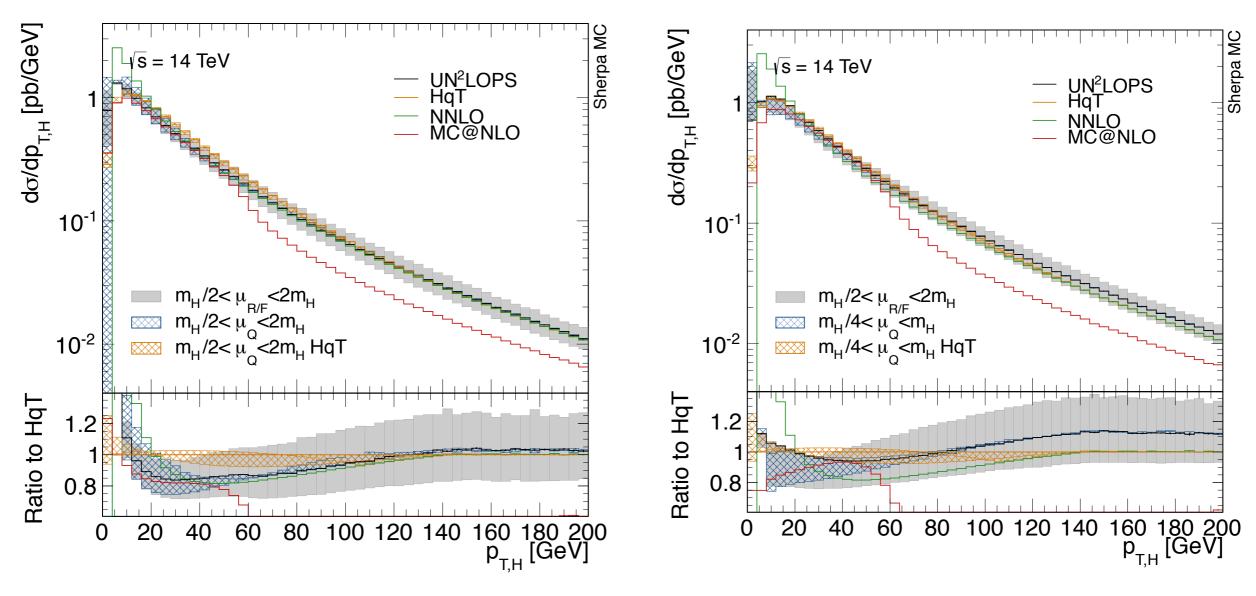
# Back Up

## Higgs pT distribution

**HqT: state-of-the-art NNLO+NNLL** 

Bozzi, Catani, De Florian, Ferrera, Grazzini, Tommasini

Hoeche, YL, Prestel arXiv:1407.3773



- Harder pT spectrum in "factorized" matching
- Lower resummation accuracy of UN2LOPS than HqT